

# Quantifying the impact of subsurface in-situ observations at important Arctic and Nordic Seas gateways on the Arctic Supolar gyre sTate Estimate

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Estimating the Circulation and Climate  
of the Ocean

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*ASOF meeting, 24-26 April 2019, Copenhagen.*



# Focus

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## Representativeness of ocean observations:

A recurring issue in the analysis and interpretation of observational data, as well in the use of these data for model validation and data assimilation, is how their representativeness in space and time are dealt with. This issue is of particular relevance for in-situ data such as oceanic measurements from profiling devices or time series data from mooring locations.

... dealing with questions related to representativeness and uncertainties in observations, what these mean for the observational analysis as well as the usefulness of the data in modelling, and ways forward in resolving those issues in particular in regions of sparse data coverage.

# Outline

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- ❑ Frameworks:
  - Ocean State Estimation / Data Assimilation
  
- ❑ Uncertainty
  
- ❑ Measurements at gateways as constraints

# What is data assimilation?

It's all about ...

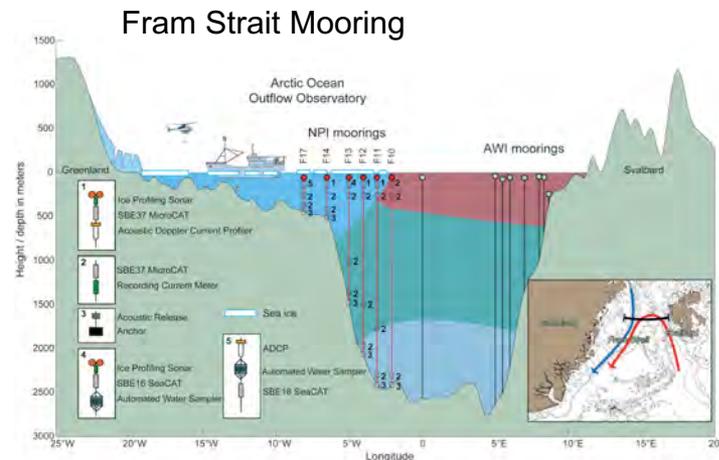
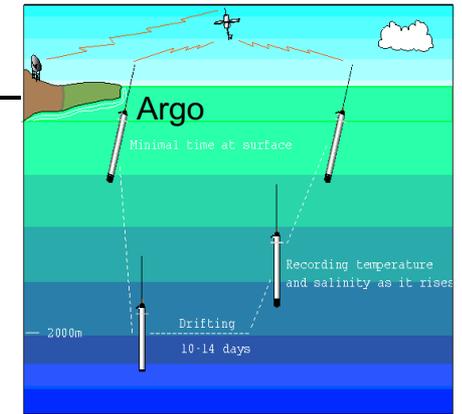
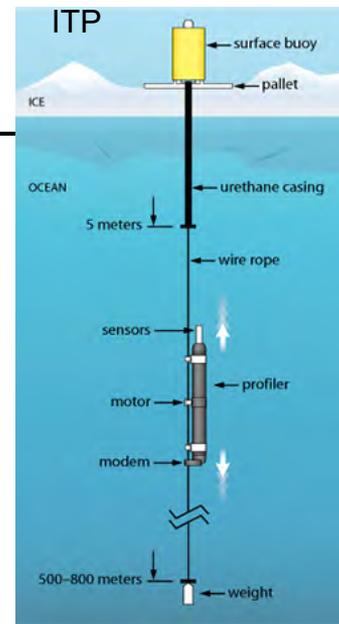
- making optimal use of,
- consistently extracting,
- or combining

information contained in *observations* and physical laws expressed through a *model*, and taking into account all *uncertainties*.

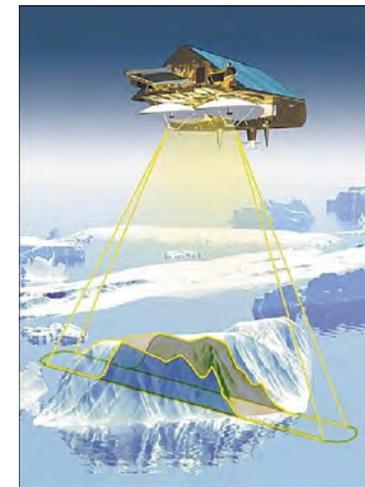
# Combine two incomplete information sources

## Observations (“data”):

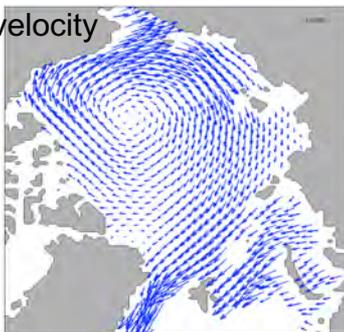
- incomplete/sparse probing of the physical system
  - spatial sampling
  - temporal sampling
  - incomplete state
- different physical variables
- heterogeneous data streams
- measurement errors
- representation errors (later)



Cryosat-2



Ice velocity



## Combine two incomplete information sources

### Physical model:

- representation of time-evolving state via equations of motion, conservation laws, theory, ...
- An interpolator
- **uncertainties/errors:**
  - initial conditions
  - boundary conditions (surface, bottom, lateral)
  - model parameters
  - “model errors” (formulation, discretization, ...)

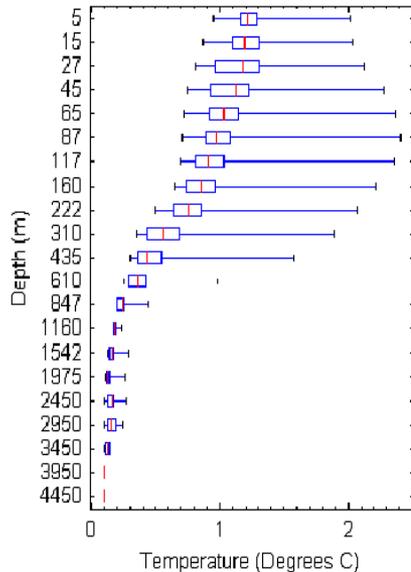
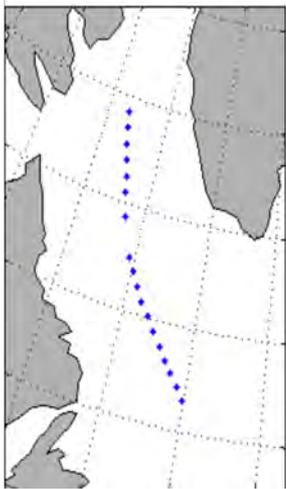

$$\begin{aligned}\frac{D\vec{v}_h}{Dt} + f\hat{\mathbf{k}} \times \vec{v}_h + \frac{1}{\rho_c} \nabla_z p &= \vec{\mathcal{F}} \\ \epsilon_{nh} \frac{Dw}{Dt} + \frac{g\rho}{\rho_c} + \frac{1}{\rho_c} \frac{\partial p}{\partial z} &= \epsilon_{nh} \mathcal{F}_w \\ \nabla_z \cdot \vec{v}_h + \frac{\partial w}{\partial z} &= 0 \\ \rho &= \rho(\theta, S) \\ \frac{D\theta}{Dt} &= Q_\theta \\ \frac{DS}{Dt} &= Q_s\end{aligned}$$

# Misfits & Jacobian

Three important ingredients are needed for state estimation:

1. the model
2. the data
3. "useful"/credible uncertainty estimates

$$J = \sum_{t=1}^{t_f} [y(t) - \mathbf{E}(t)\mathbf{x}(t)]^T \mathbf{R}(t)^{-1} [y(t) - \mathbf{E}(t)\mathbf{x}(t)] + [\mathbf{x}_0 - \mathbf{x}(0)]^T \mathbf{P}(0)^{-1} [\mathbf{x}_0 - \mathbf{x}(0)] + \sum_{t=0}^{t_f-1} \mathbf{u}(t)^T \mathbf{Q}(t)^{-1} \mathbf{u}(t)$$



$J = f(a, b, \dots)$ ,  $a, b$ : parameters

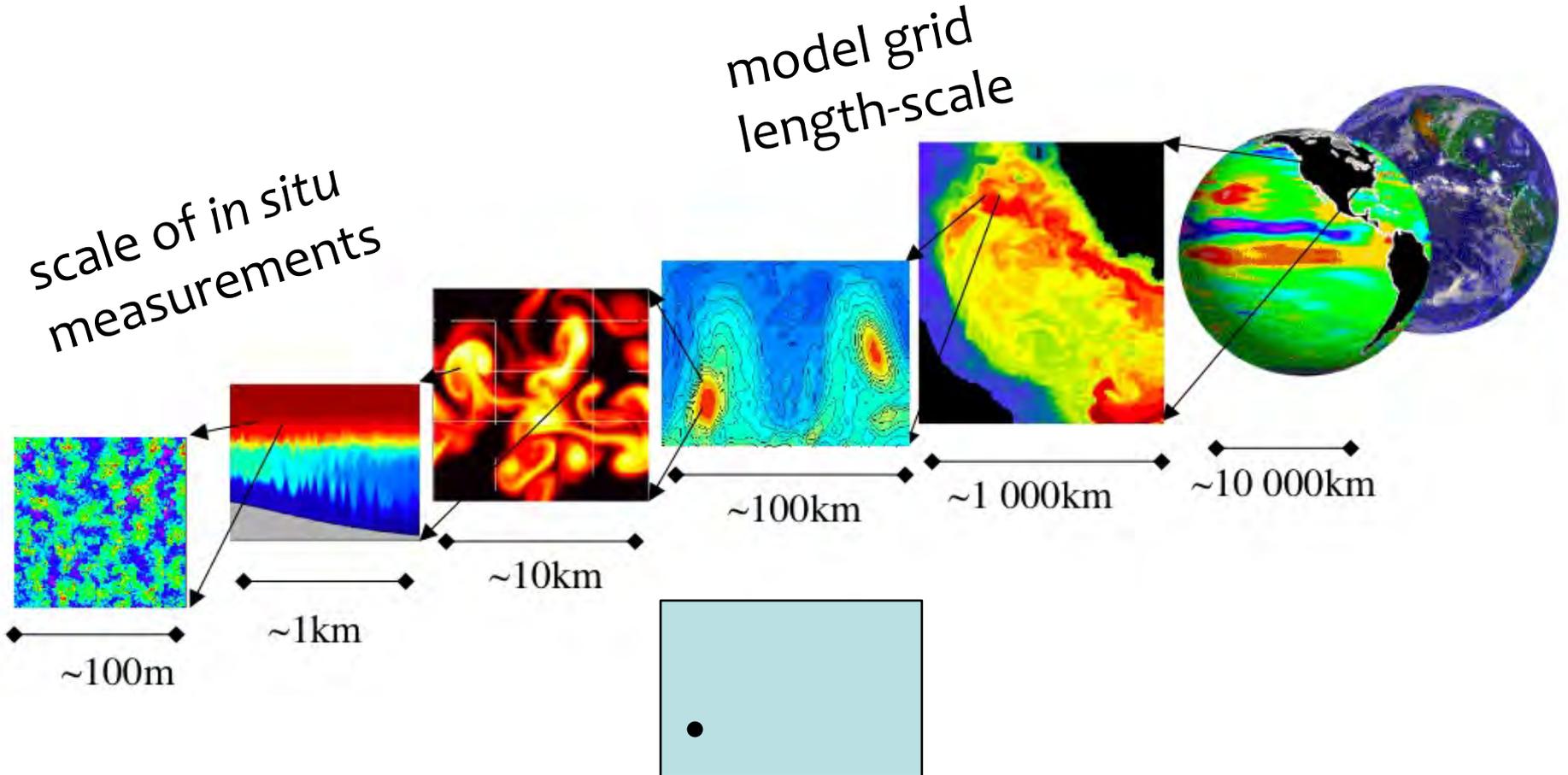
$$\delta J = \frac{\partial J}{\partial a} \delta a + \frac{\partial J}{\partial b} \delta b + \dots$$

If want to reduce  $J$  (misfits), adjust model parameters  $\delta a, \delta b, \dots$  within **error bounds**

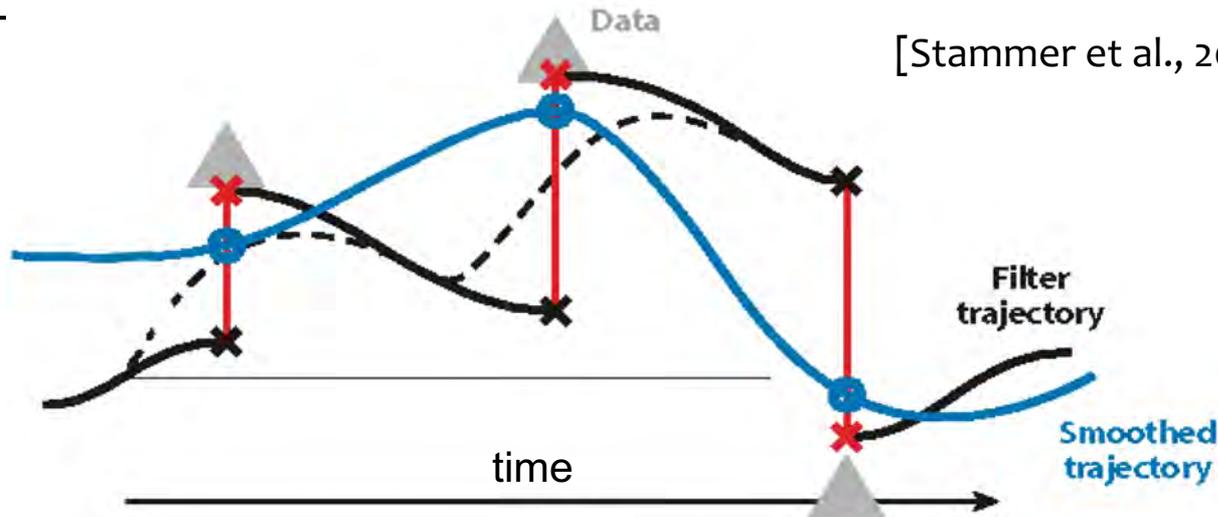
# Uncertainty quantification

how to represent variability?

→ uncertainty



# Data Assimilation can mean very(!) different things to different people



## State Estimation (smoother/adjoint):

- Bring all observations into a dynamically consistent description of the past and recent time-varying ocean circulation.
- Strictly obeys model physics at all time
- Study ocean dynamics and variability, global-scale and regional energy, heat, and water budgets.
- Decadal to multi-decadal timescale.

## Data Assimilation (filter):

- Bring all observations into a model for the purpose of prediction / forecasting
- Model updates can break conservation law.
- Update: weighting between prior knowledge and data-model misfits
- Initialization, operational
- days to months timescale

Science goal / application → determines the framework

# ASTE – Release 1.5

- Adjoint-based (nonlinear inversion) state estimation
- Mean & time-varying ocean & sea ice states
- Arctic – Subpolar gyre exchange
- Optimization period: **2002-2017**

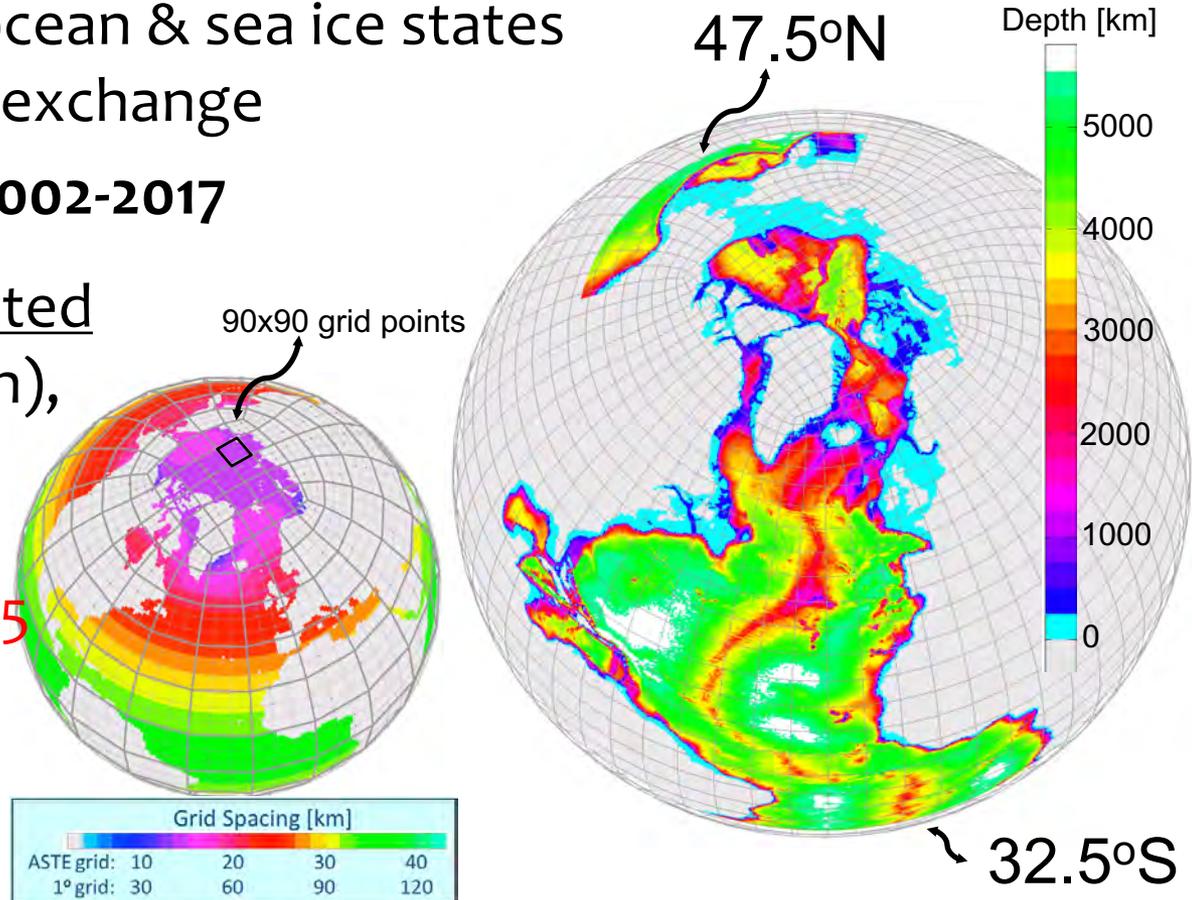
- Initial conditions: adjusted
  - WOA14 spin-up (ocean),
  - PSC spin-up (ice)

- Forcing: adjusted JRA55

- OBCs: ECCO-v4

- Control variables:

- initial conditions
- time-varying atmospheric state,
- 3-D ocean mixing parameters



# Primary data constraints:

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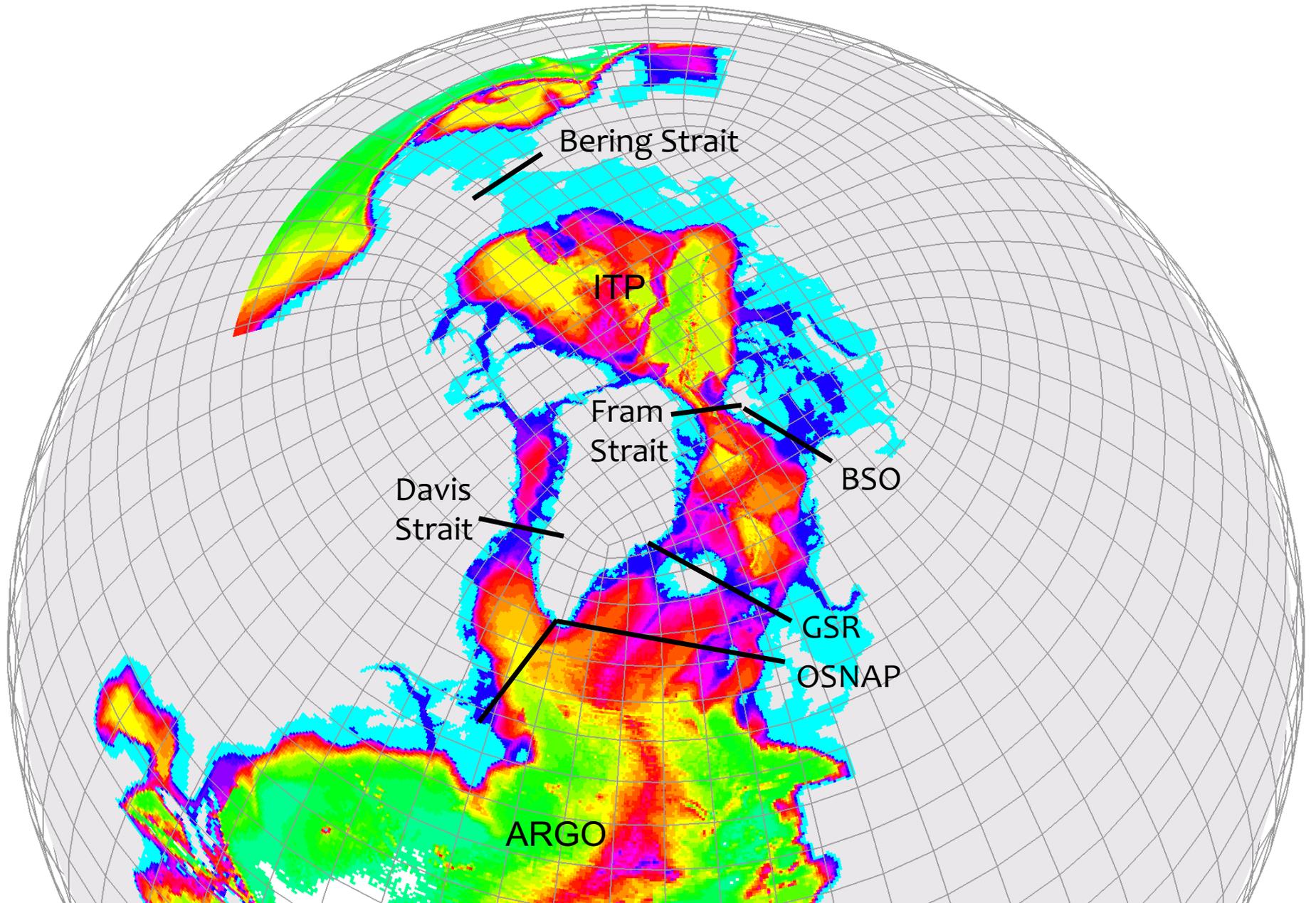
## Low latitudes:

- ECCO-v4 standard obs.  
(SSH, SST, Argo, XBT, CTDs, seal, mean DMT)
- Line-W (John Toole), Gulf Stream (Robert Todd), AR07 lines, ICES database

## High latitudes:

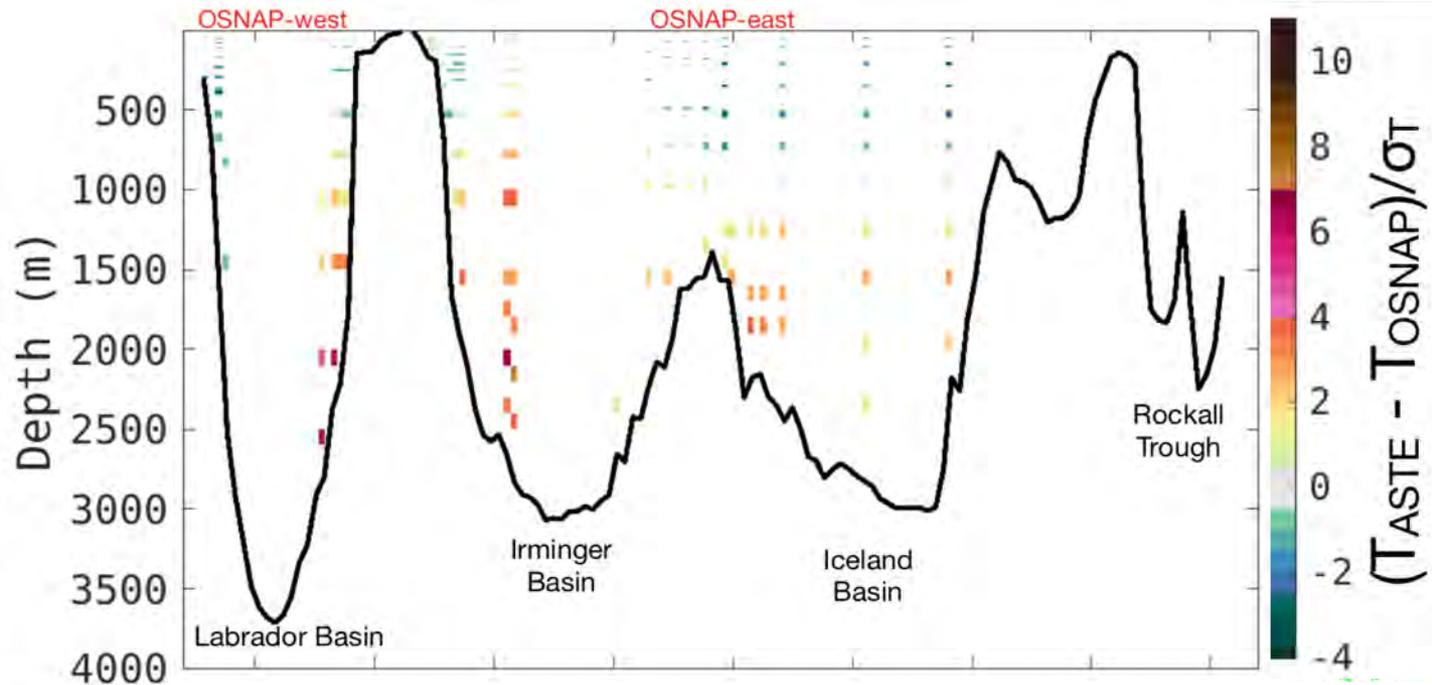
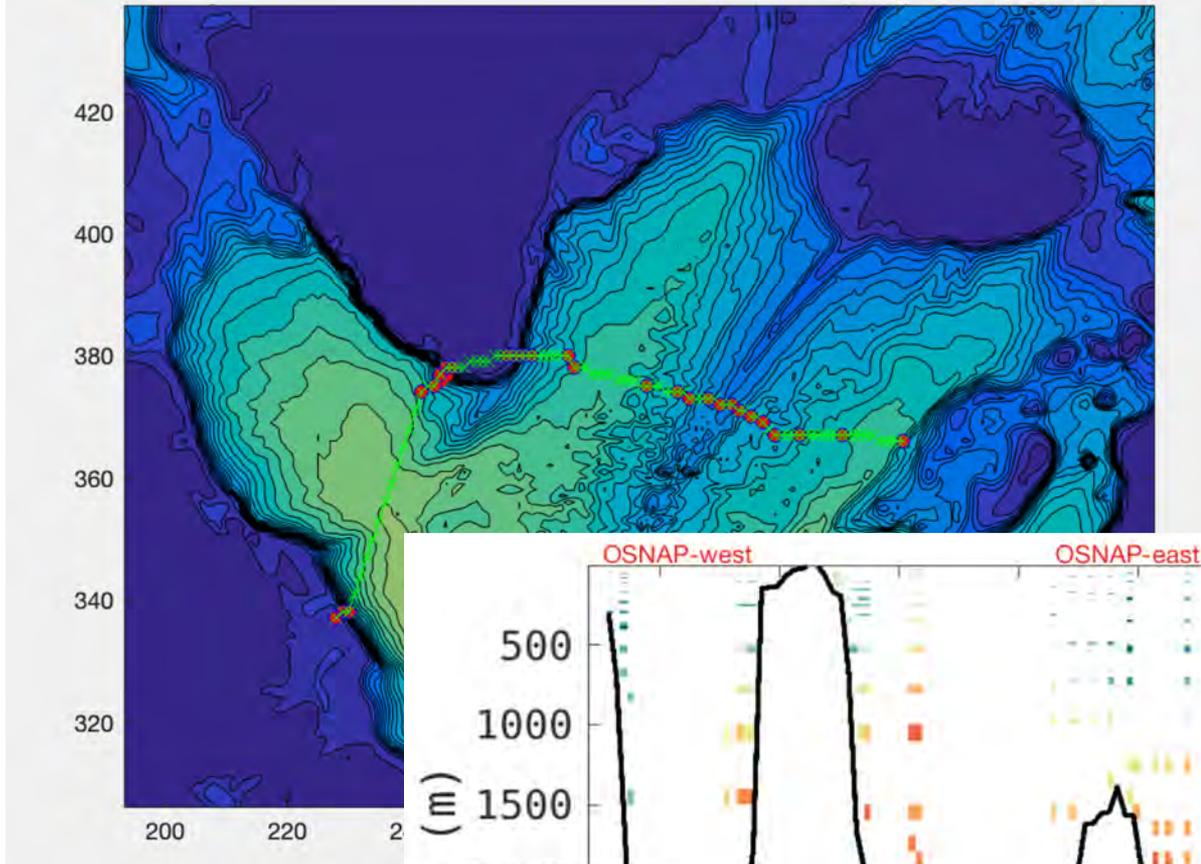
- Sea ice:
  - concentration (OSISAF, daily, 2002-2017)
  - thickness (ICESat, CryoSat, SMOS)
  - ice drift
- ocean T/S/U/V  
e.g., ITP, NABOS/CABOS, BGEP (2002-2017)
- Arctic main gateways: Fram, Davis, Bering straits, etc.

# Gateways



# Example of constraints: OSNAP

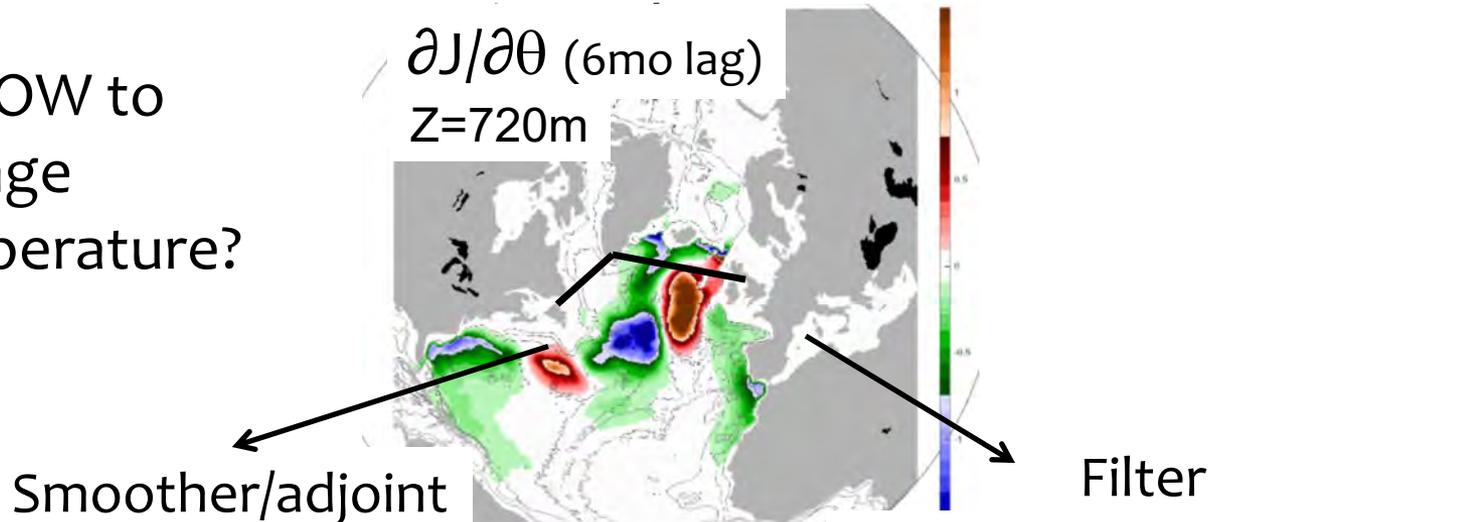
Figures courtesy of  
Helen Pillar



# State Estimation (smoother) vs. Data assimilation (filter):

Positive  $\partial J/\partial\theta$  : If want  $\downarrow J$ , then  $\downarrow \theta$  at these locations.

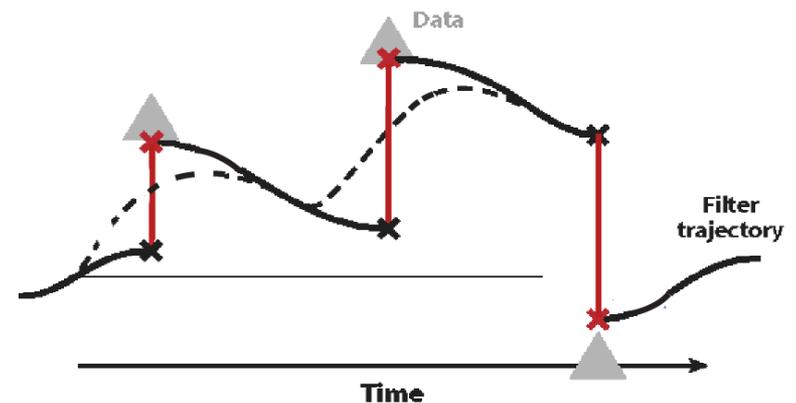
Q. HOW to change temperature?



Change the temperature!

Adjust “control parameters”,  
e.g., internal mixing,  
surface forcings  
initial conditions

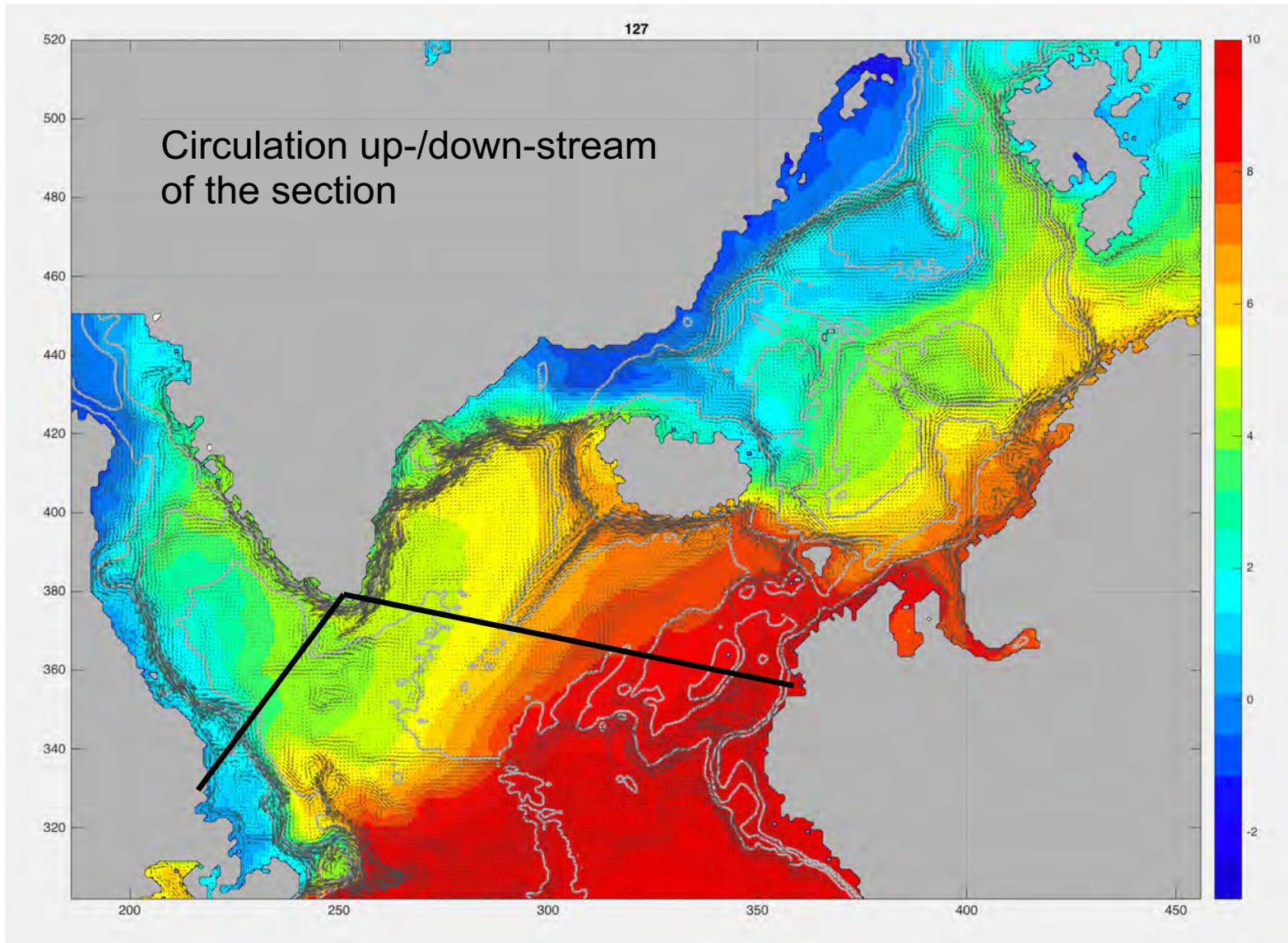
Capture processes upstream



Violates conservation laws

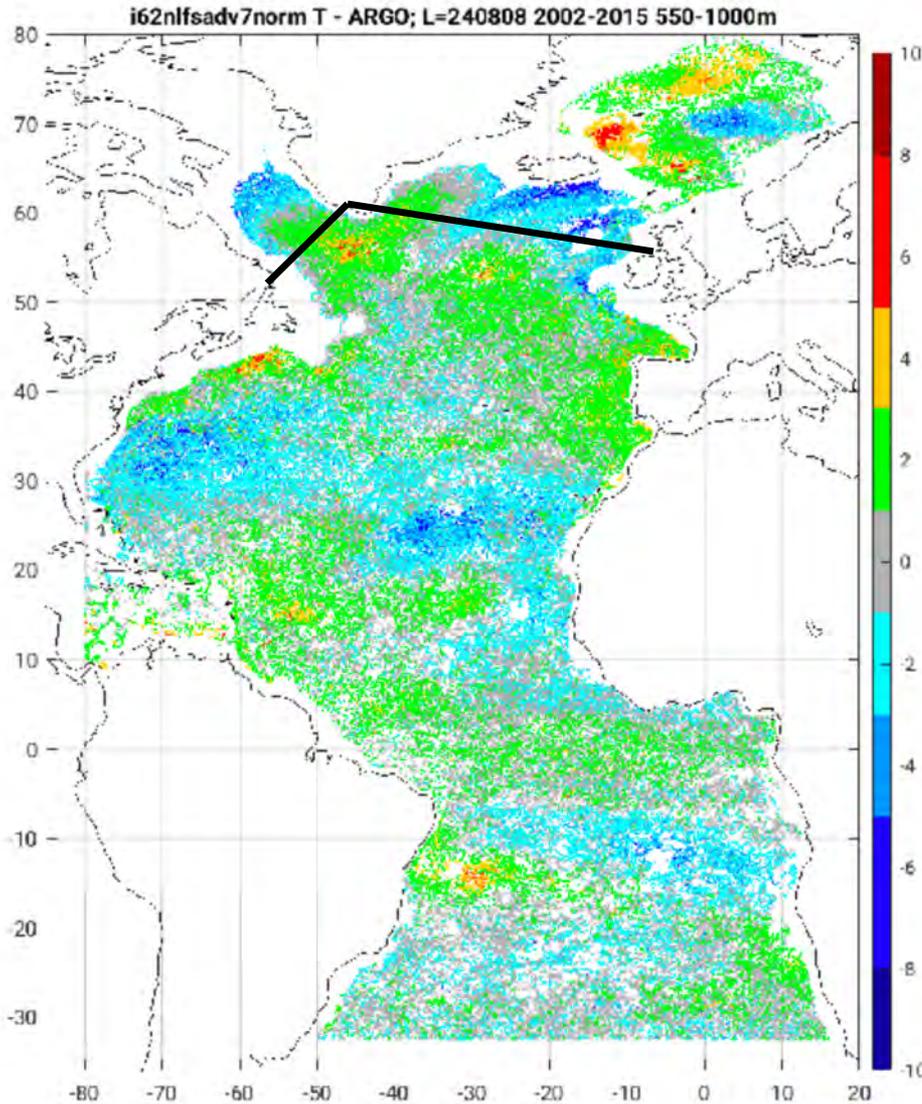


# What happens up-/down-stream of OSNAP?



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## Argo data



### Gateways:

- Boundary currents
- Exchanges between basins

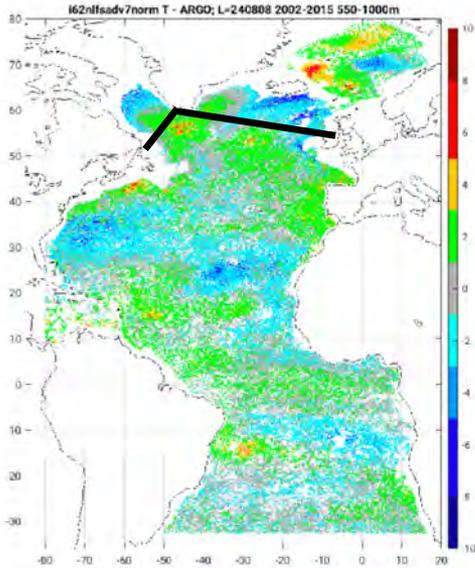
### Fits to observations:

- Need to be consistent with watermasses up-/down-stream

Ensure dynamical consistency?  
(no jumps, no unknown source/sinks)

Allow for representation errors

# What happens up/down-stream of OSNAP?



(larger) Representation vs (smaller) obs errors

## Smoothers (adjoint)

- Adjust uncertain input parameters
- More\*\* weights on representation errors
- Not nesc fitting obs point-wise (focus on integrated quantities)

## Filters

- Adjust  $T(t)$ ,  $S(t)$
- More\* weights to obs
- Better fit obs point-wise

Transports & exchanges at gateways?

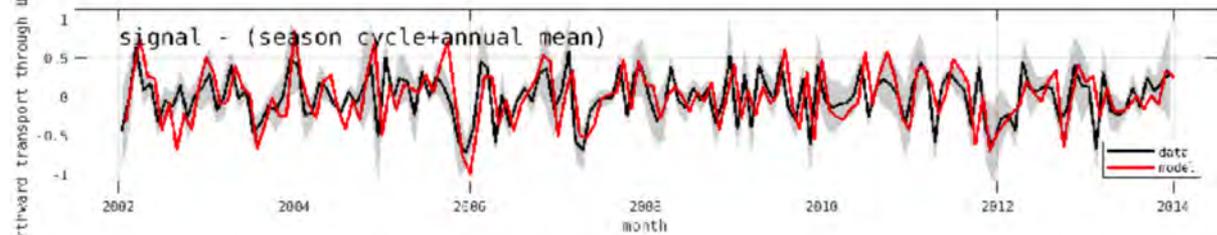
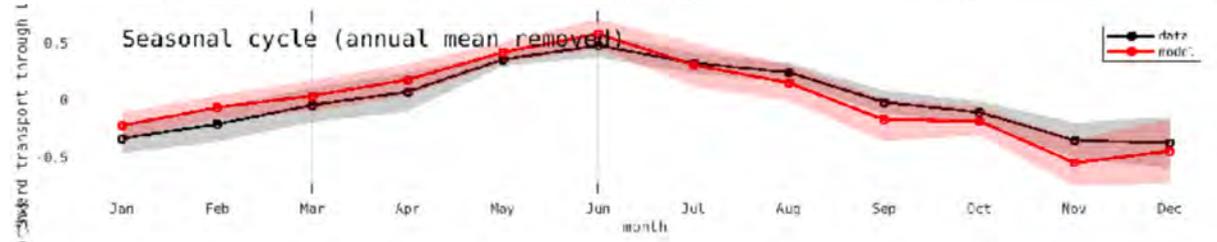
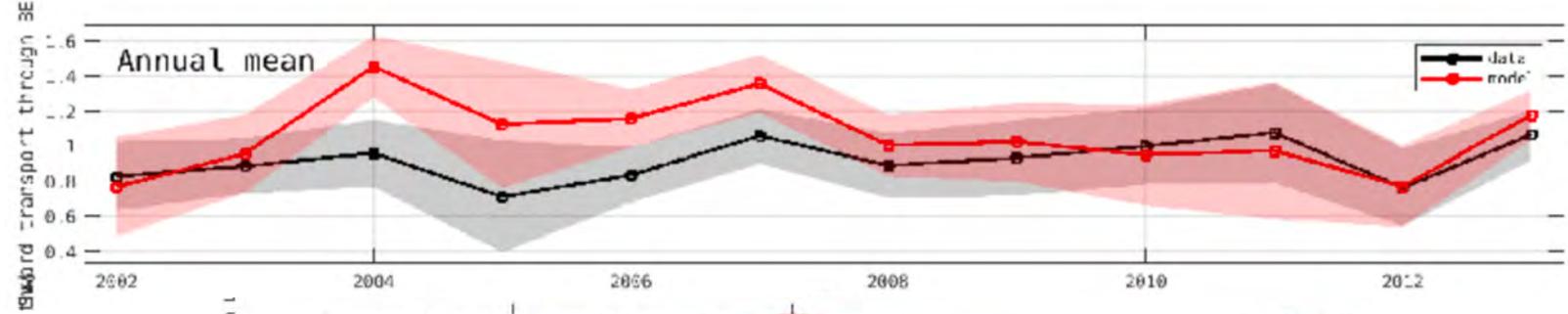
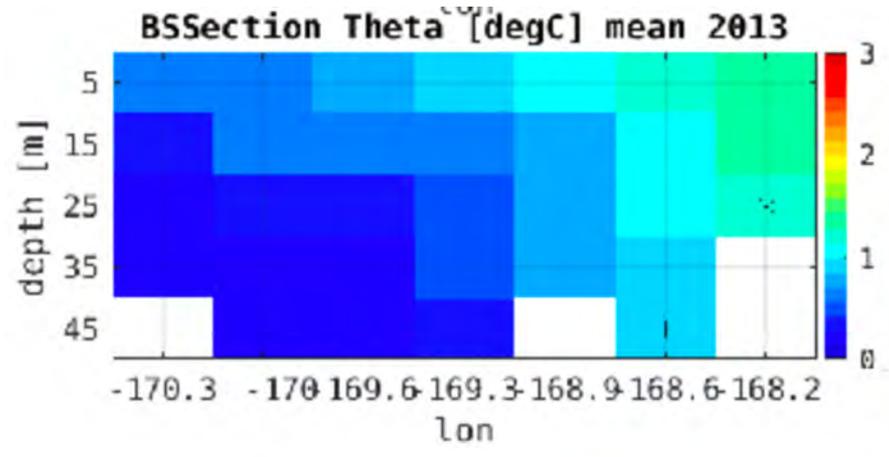
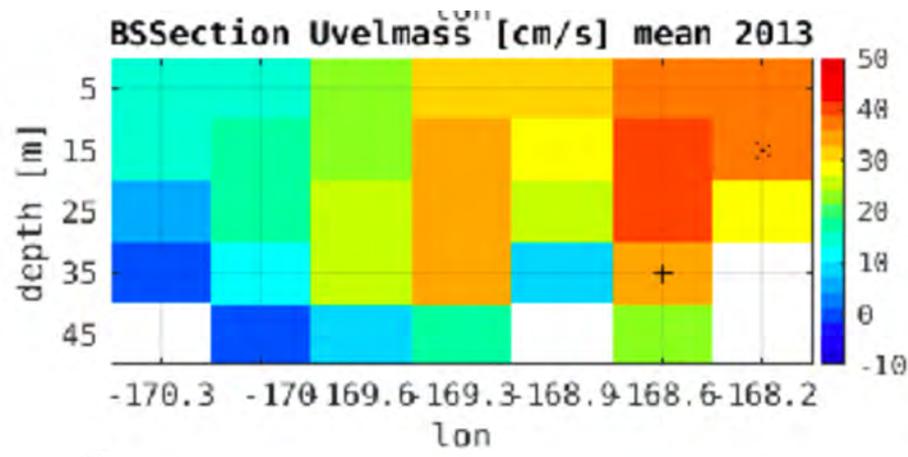
- Conserving

- Unknown sources/sinks  
- Meaning of integrated transports?

\* trust obs more → put more emphasis on observations to adjust  $T(t)$ ,  $S(t)$

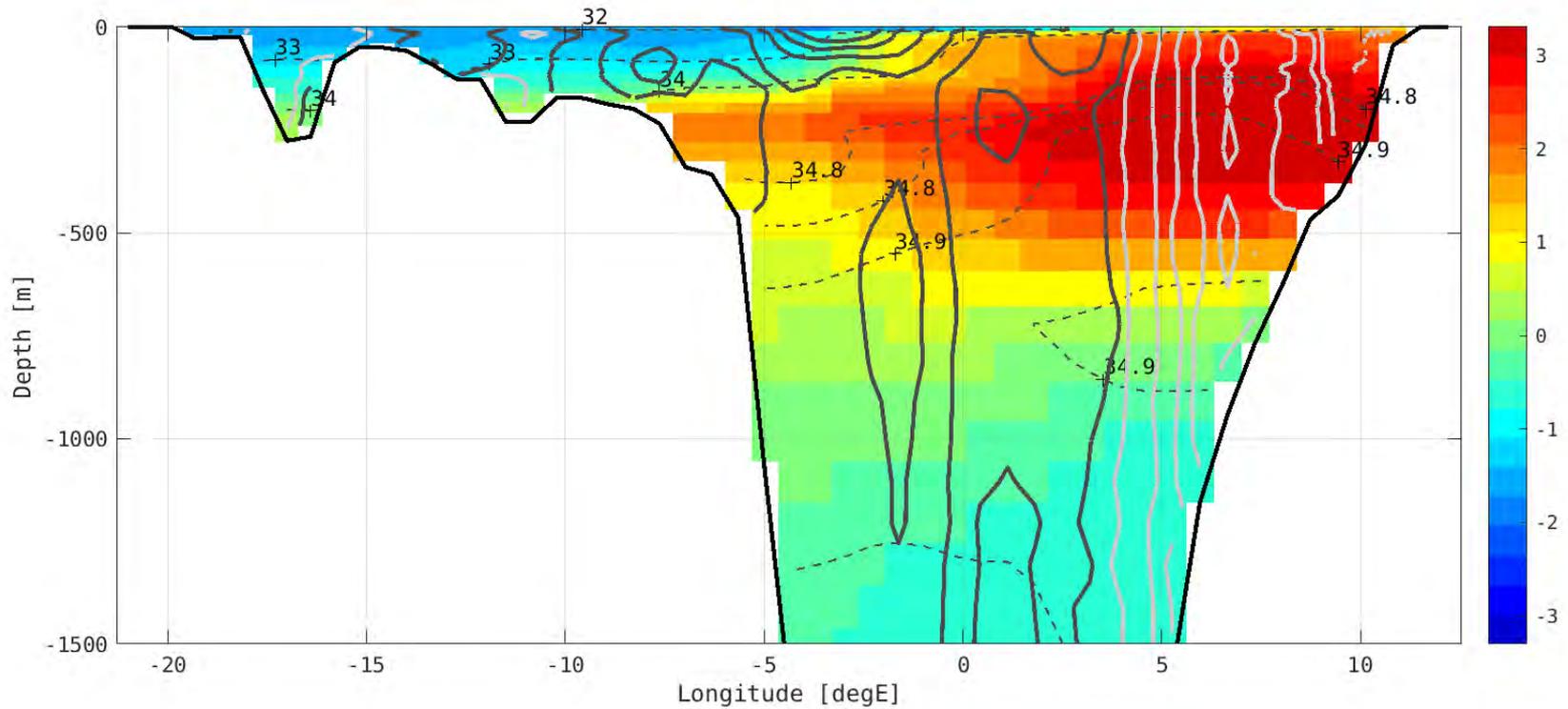
\*\* rely on model (imperfect) physics and its representation errors  
(not practical for real-time operational applications)

# Example of constraints: Bering Strait

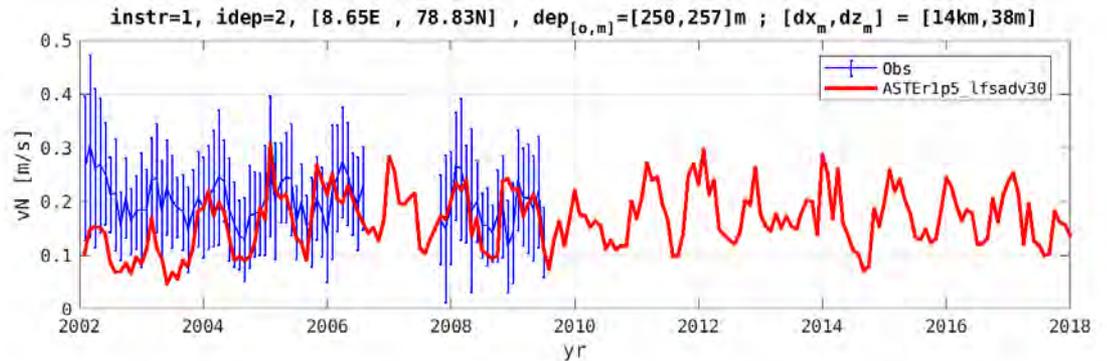
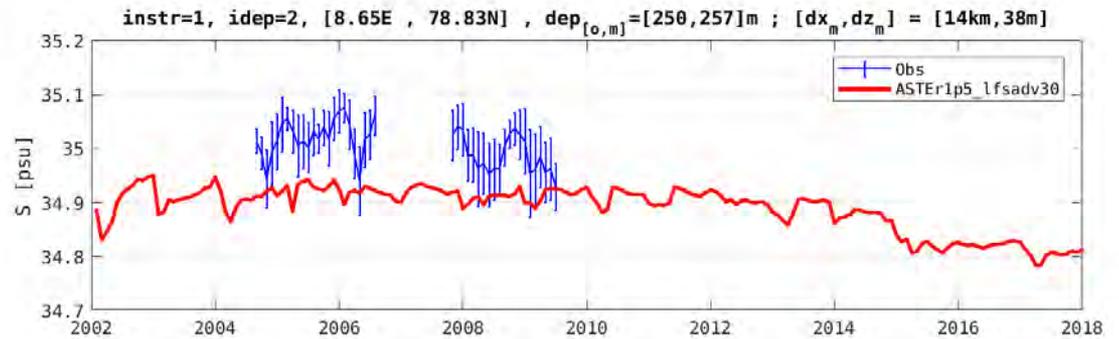
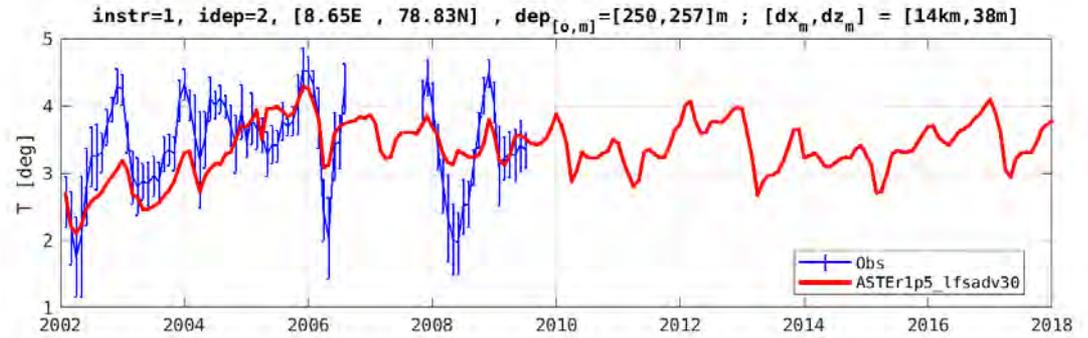
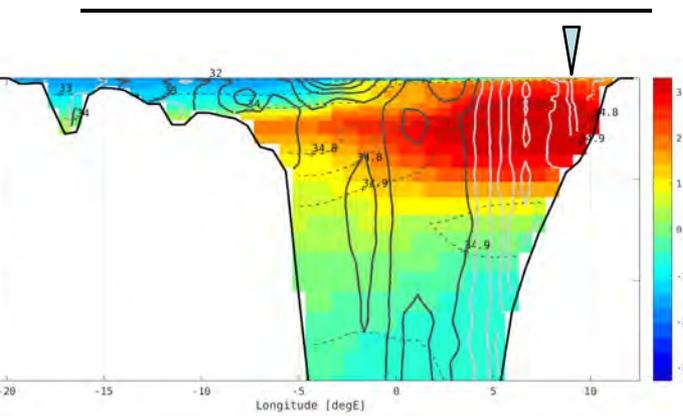


# Example of constraints: Fram Strait

ASTER1p5 , 2003–2017 mean

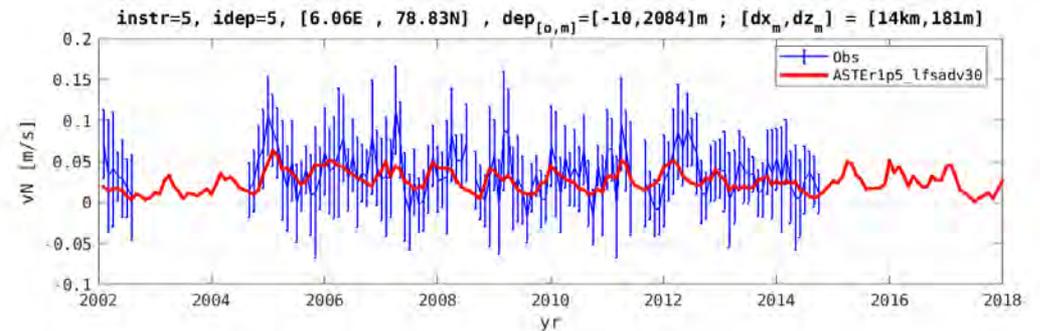
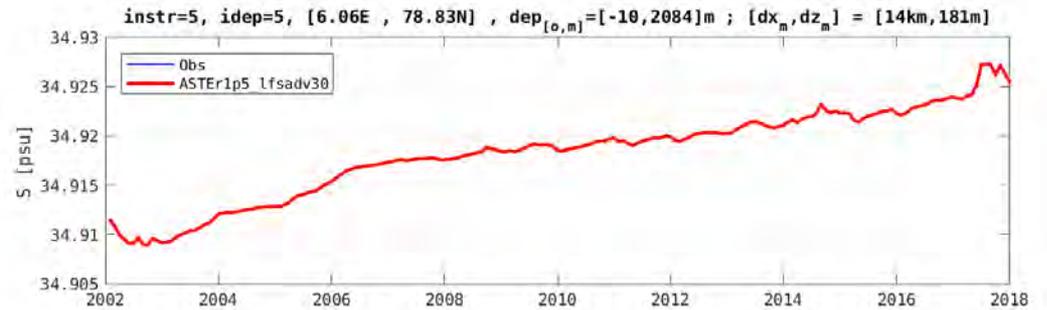
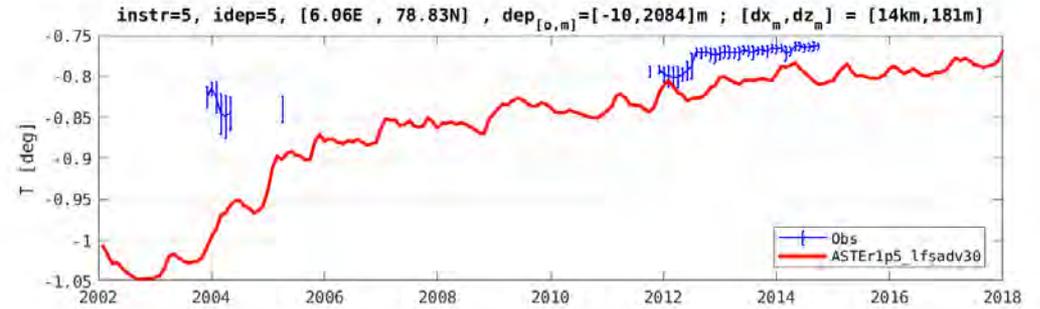
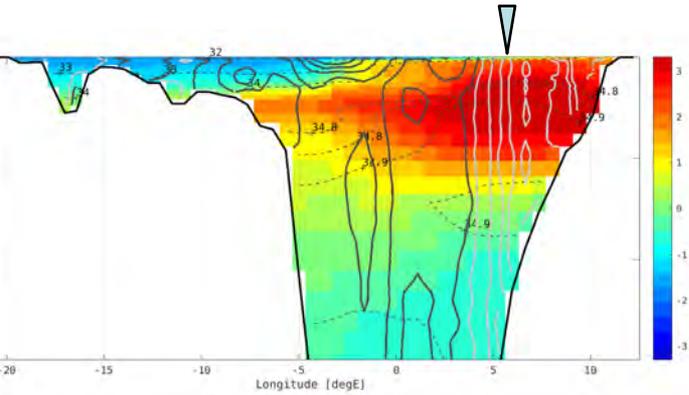


# Example of constraints: Fram Strait

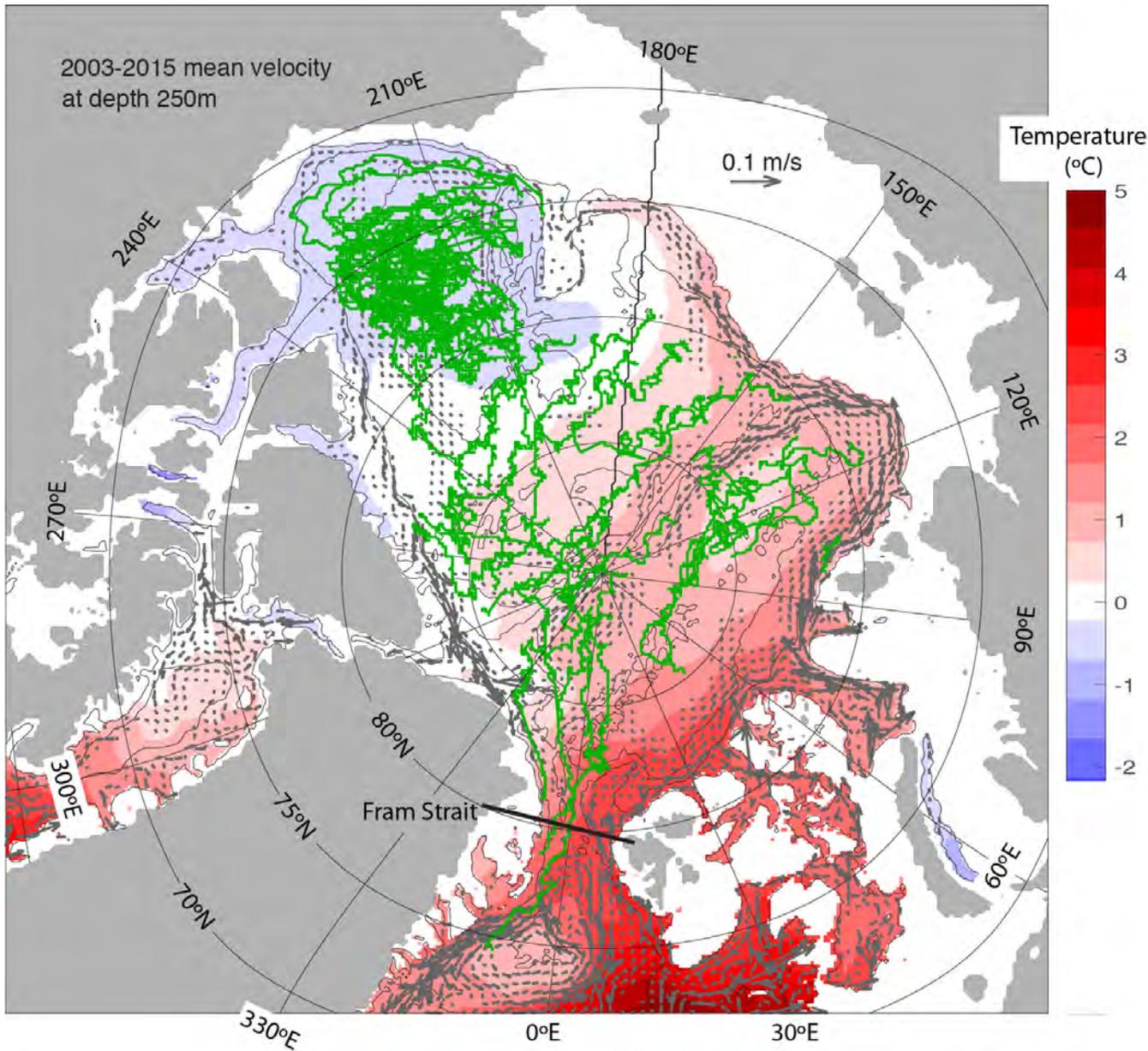


Boundary current strength?  
T/S properties?

# Example of constraints: Fram Strait



# Downstream of Fram Strait

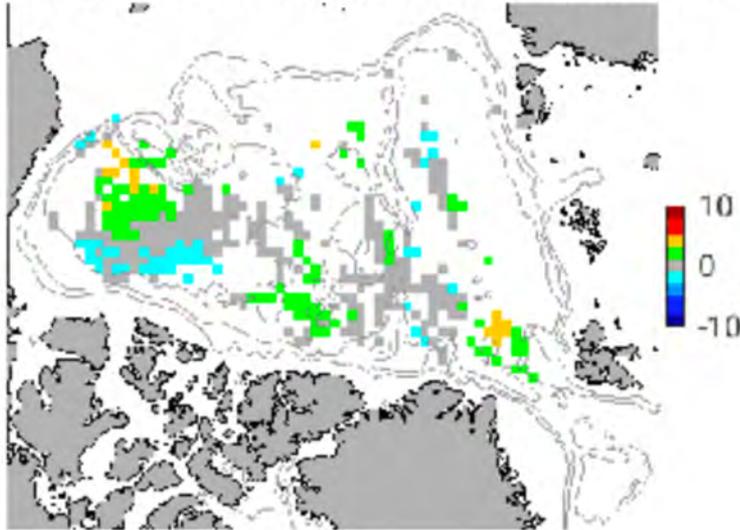


Requirement:

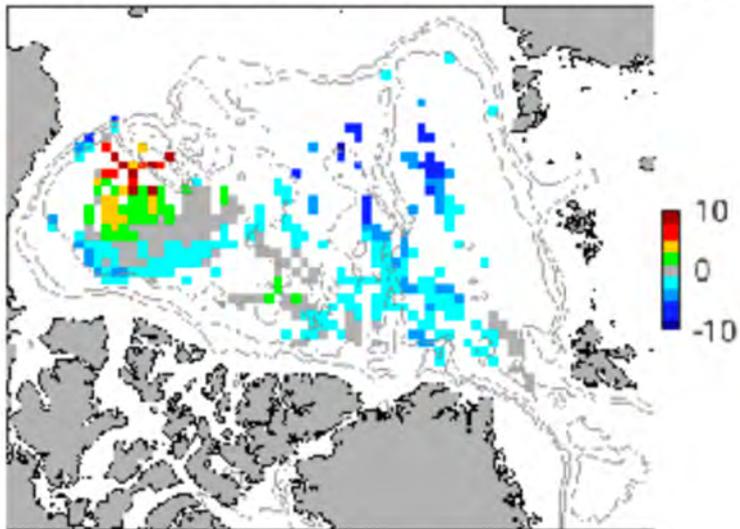
Consistency between Fram Strait transports & watermass much further downstream in the Canada Basin

# Downstream of Fram Strait

2004-2016 mean i62nlfsadv7 norm T minus ITP



2004-2016 mean i62nlfsadv7 norm S minus ITP



Requirement:

Consistency between Fram Strait transports & watermass much further downstream in the Canada Basin

→ Decadal time-scale

→ Taken into account model representation errors

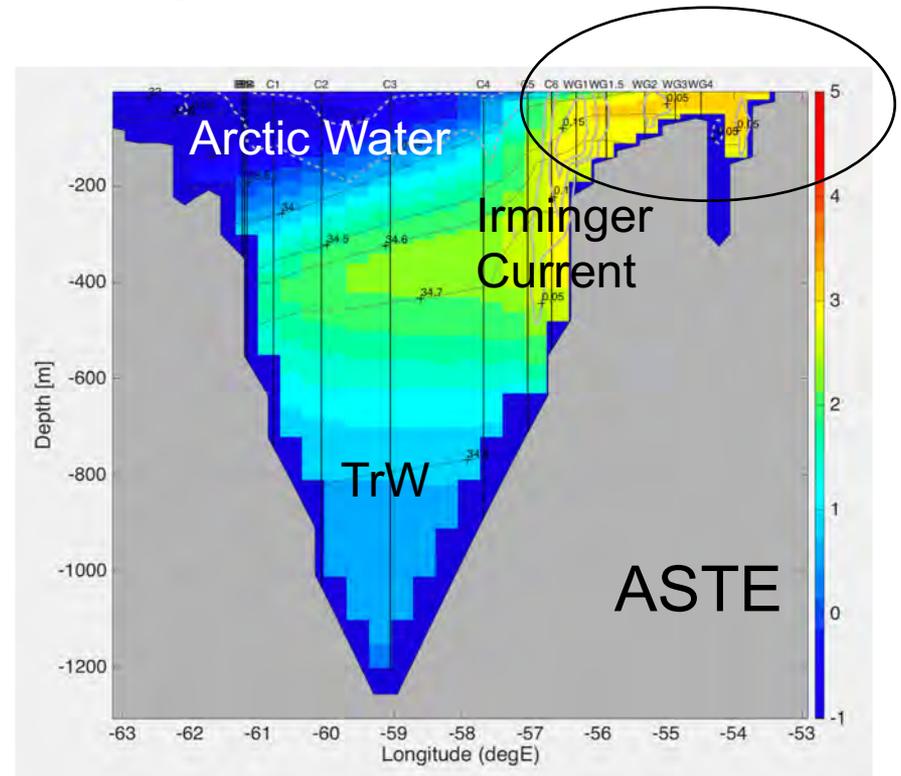
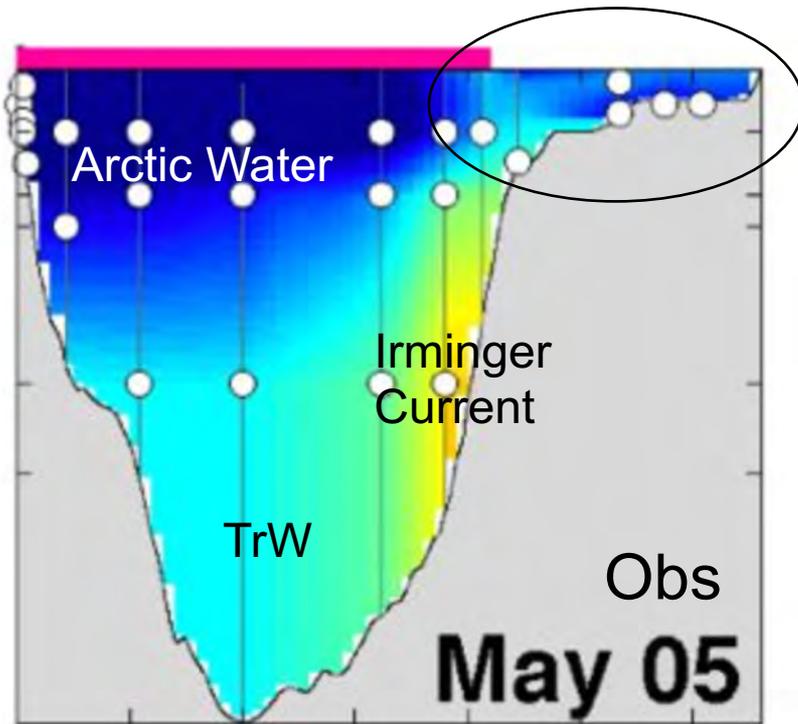
→ account for **non-uniqueness** of adjustments to uncertain parameters

→ Not “over-fitting” obs at gateways (and elsewhere)

# Example of constraints: Davis Strait

Source:

- (a) East Greenland Current (**exiting from Fram Strait**)
- (b) Greenland glacial melt (solid and liquid)



Problem much further upstream that needs to be addressed?  
Missing source term?

# Use of observations as constraints

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- State estimates:
  - follows conservation laws (momentum, tracers, mass)
  - dynamical interpolator of observations at different space/time scales
  - source/sink accounted for → budgets, circulation
  - always have bias/representation errors
- Usefulness of observations as constraints:
  - understand processes up-/down-streams of gateways
  - importance of continuous sub-surface measurements
  - Sparseness of obs: lack of velocity constraints
- Comparison with care
  - integrated quantities vs point-to-point
  - model: representation errors. Obs: interpolation assumptions